

# Intermediary Balance Sheets and the Treasury Yield Curve

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# Treasury “Inconvenience”?

## Pre-GFC:

- ▶ Treasury bonds were convenient (low yield relative to swap rates)
  - ▶ i.e. positive swap spreads (swap rate - Treasury yield)
- ▶ Covered interest parity (CIP) violations were roughly zero

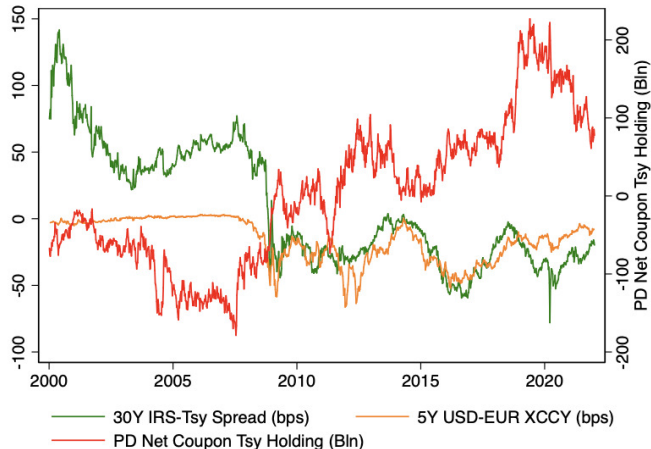
## Post-GFC:

- ▶ Treasury bonds are inconvenient (negative swap spreads)
- ▶ CIP violations are non-zero

This paper: unified framework to explain the swap spread, dealers' positions, and CIP deviations

- ▶ Sign of position, swap spreads coincide (“regimes”)
- ▶ Regime determines effects of QE/QT and other policies

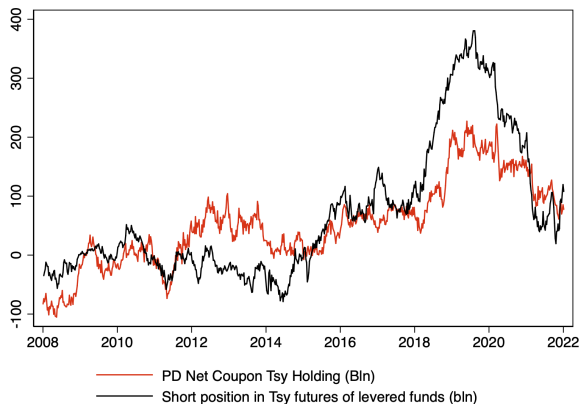
# Dealer Treasury Position, Swap Spreads, and CIP Deviations



- ▶ Known Facts: (i) swap spread pos. to neg. and (ii) CIP zero to neg.
- ▶ New Facts: (i) dealer net position neg. to pos. and (ii) CIP/swap spread correlation

# Dealers and the Implied Levered Investors' Holdings

- ▶ Levered investors rely on dealers' balance sheet for repo funding to finance their Treasury holdings.
- ▶ Dealer's own holdings are quite correlated with the implied relative-value hedge fund holdings (long cash Treasury bonds, short Treasury futures).



# What We Do?

1. Using OIS rate and CIP deviations to construct a dealer-long and dealer-short curve for Treasury bonds
  - ▶ The actual yield switched from the dealer-short to the dealer-long curve, consistent with the change in the net position.
2. Two-period, two-market equilibrium model (Treasury bonds and synthetic dollars)
  - ▶ Endogenous dealer position
  - ▶ Policy implications

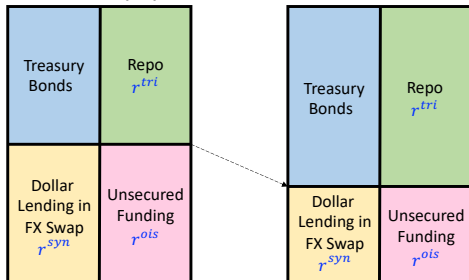
# Related Literature

- ▶ Jermann (2020): calibration in which dealer constraints explain negative swap spreads
  - ▶ We measure quantities, quantify constraints with CIP, explain quantity-slope correlation
- ▶ He, Nagel, and Song (2021): shares focus on dealer leverage constraints and swap-treasury spreads.
  - ▶ They compare GFC vs. COVID crisis events; explanation: sign of customer shocks
  - ▶ We compare pre- and pre-GFC periods; explanation: regimes, no change in shocks
- ▶ Our view: Treasuries are convenient to clients but inconvenient to intermediaries.
  - ▶ Treasury convenience: Longstaff (2004), Krishnamurthy and Vissing-Jorgensen (2012), Greenwood, Hanson, and Stein (2015), etc.
- ▶ The market equilibrium model in Hanson, Malkhozov, and Venter (2022) is similar in spirit to ours but focuses on the swap market. Complementary approach.
- ▶ Our arbitrage view of dealer bond trading contrasts the return-seeking view of commercial banks in Haddad and Sraer (2020).

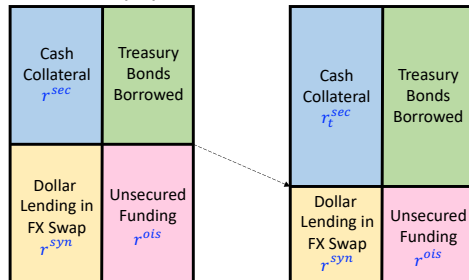
# 1. Dealer-Long and Dealer-Short Curves

# Balance-Sheet Neutral Treasury Trading Strategies

(A) Long Treasury



(B) Short Treasury





# A Simple Model of Dealers and Arbitrage

- ▶ Consider a dealer that chooses between trading a single  $n$ -period zero-coupon Treasury bond, v.s. CIP arbitrage.
- ▶  $\mathbb{Q}$  reflects dealer's SDF for zero-cost, zero-balance-sheet trades (i.e. derivatives).
- ▶ Define the expected next-period bond price as

$$p_{\mathbb{Q}} \equiv \exp(-(n-1)y_{\mathbb{Q}}) \equiv E^{\mathbb{Q}}[\exp(-(n-1)y_{n-1,1})]$$

# Dealer's Problem

$$\begin{aligned}
 & \max_{q^{bond}, q^{syn}} \left( \underbrace{e^{r^{syn}} - e^{r^{ois}}}_{\text{synthetic lending spread}} \right) \cdot q^{syn} \\
 & + \left( \underbrace{\frac{p_Q}{e^{-ny}}}_{\text{sell after one period}} - \underbrace{e^{r^{tri}}}_{\text{secured financing}} \right) \cdot \max\{q^{bond}, 0\} \\
 & + \left( \underbrace{e^{r^{sec}}}_{\text{earn security lending rate}} - \underbrace{\frac{p_Q}{e^{-ny}}}_{\text{buy back after one period}} \right) \cdot \max\{-q^{bond}, 0\}
 \end{aligned}$$

subject to balance sheet constraint:

$$|q^{bond}| + q^{syn} \leq \bar{q}$$

- ▶ We avoid corner solutions by assuming dealers do CIP arbitrage, i.e.,  $q^{syn} > 0$ .

# The Long Regime

- ▶ Long regime (the optimal  $q^{bond} > 0$ ): dealer FOC implies

$$e^{-ny} = \frac{p_{\mathbb{Q}}}{e^{r^{tri}} + (e^{r^{syn}} - e^{r^{ois}})}.$$

- ▶ Denote the long-regime yield as  $y^l$ . Consider a special case of one-period bond ( $n = 1, p_{\mathbb{Q}} = 1$ ). The log-linearized version is

$$y^l \approx r^{syn} - r^{ois} + r^{tri},$$

or equivalently,

$$\underbrace{r^{ois} - y^l}_{\text{swap spread}} \approx - \underbrace{(r^{syn} - r^{ois})}_{\text{balance sheet cost}} + \underbrace{(r^{ois} - r^{tri})}_{\text{funding benefit}}.$$

# The Short Regime

- ▶ Short regime (the optimal  $q^{bond} < 0$ ): dealer FOC implies

$$e^{-ny} = \frac{p_{\mathbb{Q}}}{e^{r^{sec}} - (e^{r^{syn}} - e^{r^{ois}})}.$$

- ▶ Denote the short-regime yield as  $y^s$ . Consider a special case of one-period bond ( $n = 1, p_{\mathbb{Q}} = 1$ ). The log-linearized version is

$$y^s \approx -(r^{syn} - r^{ois}) + r^{sec},$$

or equivalently,

$$\underbrace{r^{ois} - y^s}_{\text{swap spread}} \approx \underbrace{r^{syn} - r^{ois}}_{\text{balance sheet cost}} + \underbrace{(r^{ois} - r^{sec})}_{\text{security lending cost}}.$$

# Multi-Period Net Long and Net Short Curve

- ▶ Same logic as the two-period model. All yields are now in annualized units, but each period is one month.
- ▶ Dealers must be willing to long if  $y_{n,t} \geq y_{n,t}^l$ , defined recursively by

$$e^{-\frac{n}{12}y_{n,t}^l} = \frac{E_t^Q[e^{-\frac{n-1}{12}y_{n-1,t+1}^l}]}{e^{\frac{1}{12}r_t^{tri}} + \left(e^{\frac{1}{12}r_t^{syn}} - e^{\frac{1}{12}r_t^{ois}}\right)}$$

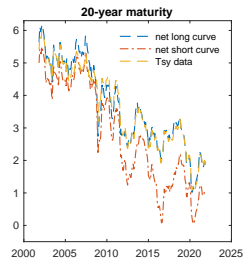
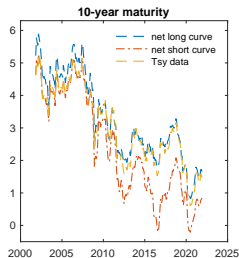
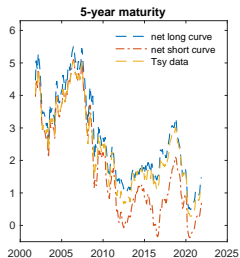
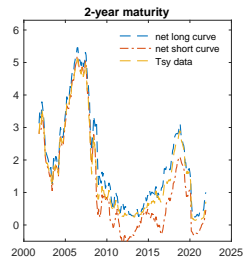
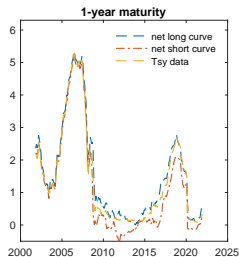
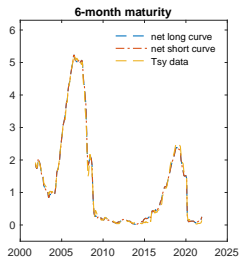
- ▶ Dealers must be willing to sell if  $y_{n,t} \leq y_{n,t}^s$ , defined recursively by

$$e^{-\frac{n}{12}y_{n,t}^s} = \frac{E_t^Q[e^{-\frac{n-1}{12}y_{n-1,t+1}^s}]}{e^{\frac{1}{12}r_t^{sec}} - \left(e^{\frac{1}{12}r_t^{syn}} - e^{\frac{1}{12}r_t^{ois}}\right)}$$

# The Term Structure Model

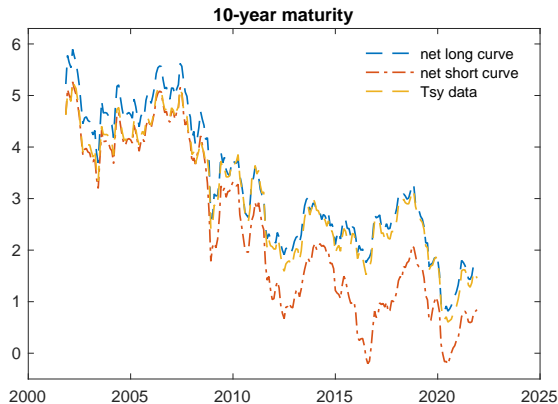
- ▶ Fit term structure model to OIS, CIP curves
- ▶ Use standard affine TS approach as in Joslin, Singleton, and Zhu (2011)
- ▶ Then construct net long and net short curves
- ▶ Key point: TS model for interpolation, Jensen's inequality, etc... Balance sheet costs + funding spreads are key inputs, determined by data

# The Net Long and Net Short Curves



# 10Y Yield pre- and post-GFC

- ▶ The actual bond yield switches from the dealer-short to the dealer-long curve, consistent with the change in dealers' position.





# Takeaways

Pre-GFC, yields were near sell arbitrage bounds (“short regime”)

- ▶ buy-sell gap much smaller due to non-binding balance sheet constraints
- ▶ Post-GFC, treasury yields are near buy arbitrage bounds (“long regime”)
- ▶ Validate arbitrage-centric view of dealer positions

Next questions:

- ▶ What caused the pre- to post-GFC changes?
- ▶ What are the implications of being in the long vs. short regime?

## 2. Equilibrium Model

# An Equilibrium Model

- ▶ Endogenous variables: (1) current  $n$ -period treasury bond yield  $y$ ; (2) synthetic dollar lending rates  $r^{syn}$ . (3) Intermediary choices  $q^{bond}$  and  $q^{syn}$ .
- ▶ Intermediaries (consolidated dealers and levered clients) optimize profit subject to constraint

$$|q^{bond}| + q^{syn} \leq \bar{q}$$

- ▶ Real-money investors (e.g., pension funds and mutual funds) demand

$$D_U^{bond} = D_U \underbrace{(ny - (n-1)y_P - y^{bill})}_{\text{Exp. Dollar Return vs Bill}}$$

- ▶ FX-hedge foreign investors (e.g., foreign life insurance companies) demand

$$D_H^{bond} = D_H \left( \underbrace{ny - (n-1)y_P - r^{syn}} \right)_{\text{Exp. Dollar Hedged Excess Return}}$$

- ▶ Each unit of bond requires synthetic financing, so  $D_H^{syn} = D_H^{bond}$ .

# Market Clearings

- ▶ Treasury market:

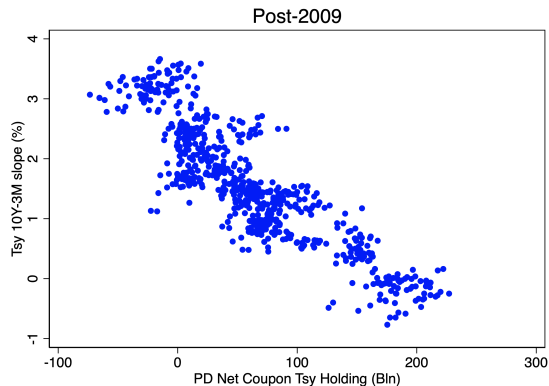
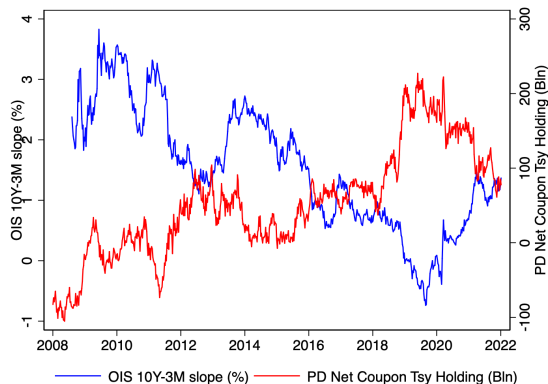
$$\underbrace{\exp(-ny)S^{bond}}_{\text{Treasury bond supply in dollars}} = q^{bond} + D_U^{bond} + D_H^{bond}$$

- ▶ Synthetic lending market:

$$\underbrace{q^{syn}}_{\text{intermediary supply of syn lending}} = D_H^{bond} + \underbrace{D^{syn}(r^{syn} - r^{ois})}_{\text{residual demand}}$$

# Dealers' Position Negatively Correlated with the Slope

- ▶ The model implies that a steeper Treasury yield slope is correlated with stronger real-money demand for Treasury, which results in a lower dealer position, and a more negative swap spread.
- ▶ Contrasts with Jermann (2020) that the dealer inventory increases in the slope.



# Key Results (Summary)

- ▶ The equilibrium is unique
- ▶ Equilibria can be classified as long/intermediate/short based on  $q^{bond}$
- ▶ Key regime determinant: bond supply and OIS term premium.
  - ▶ Bond supply high (low): long (short) regime
  - ▶ swap term premium high (low): short (long) regime
- ▶ Compare with the existing literature: IRS demand from underfunded pensions (Klingler and Sundaresan, 2019)

# Key Changes Pre/Post GFC

- ▶ Supply of Treasury bonds has increased significantly, dealer balance sheets have contracted

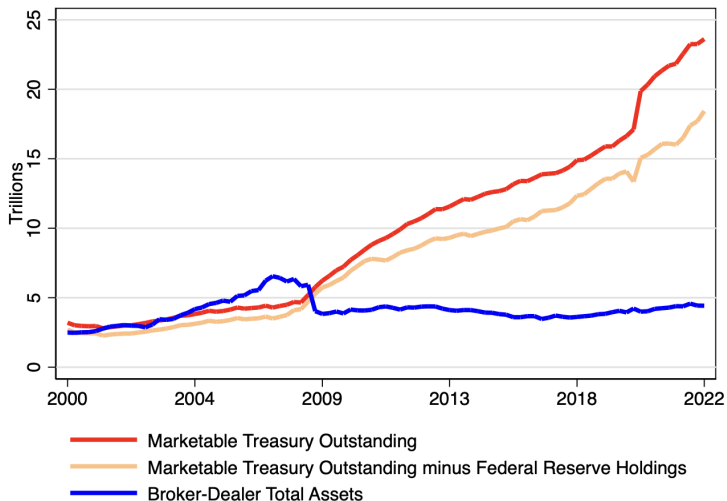


Table 1: OIS-Treasury Spreads, Pension Fund Underfunding, and Treasury Supply

	Dependent variable: $\Delta(\text{OIS-Tsy Spread})_t$ of maturity			
	30Y	10Y	5Y	2Y
$\Delta\text{UFR}_t$	-0.685** (0.339)	-0.175 (0.279)	0.163 (0.251)	-0.175 (0.233)
$\Delta\log(\text{Net Tsy}_t)$	-1.405*** (0.364)	-1.156*** (0.300)	-0.970*** (0.271)	-0.702*** (0.251)
Constant	0.018 (0.013)	0.016 (0.011)	0.013 (0.010)	0.012 (0.009)
Observations	76	76	76	76
Adjusted R <sup>2</sup>	0.218	0.165	0.126	0.092



# Regimes and Treasury Market Fragility

- ▶ Crises reduce dealer capacity  $\bar{q}$ .
  - ▶ In the short regime (pre-2009) a bad shock to intermediary balance sheet **decreases** the Treasury yield relative to swaps.
  - ▶ In the long regime (post-2009) a bad shock to intermediary balance sheet **increases** the Treasury yield relative to swaps.
  
- ▶ An explanation of the Treasury market turmoil in March 2020 (Duffie (2020)).
  - ▶ Our explanation does not rely on “selling pressure” in the Treasury market (He, Nagel, and Song (2022)). Quantifying both forces is an interesting future direction.

# Policy Implications

- ▶ Caveat: partial equilibrium, holds fixed swap and money market rates → determined by policy expectations
  - ▶ interpret Tsy yield and lending rate as **relative spreads to swaps**.
- ▶ Synthetic lending rate  $r^{syn}$  is the rate on all non-repo-financed, balance-sheet-using assets.

Policy Type	Long Regime		Short Regime	
	Tsy Yield	Lending Rate	Tsy Yield	Lending Rate
QT	↑	↑	↑	↓
↓ Term premium	↑	↑	↑	↓
SLR Exemptions	↓	↓	↑	↓
Dollar swap line	↓	↓	↑	↓

Figure 1: Primary Dealers' Treasury Position

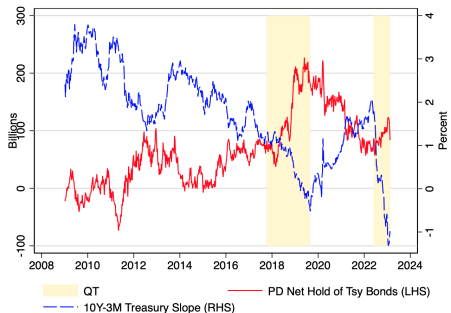
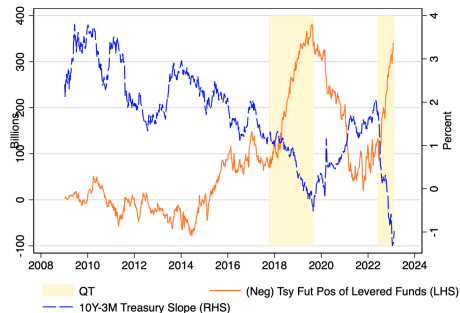


Figure 2: Implied Relative-Value Levered Investors' Treasury Position



Source: Du, Hébert and Li (updated, March 2, 2023)